## Unit 4 Facts Parallel Lines Proofs

| Corresponding Angles Theorem | If two parallel lines are cut by a <br> transversal, then the pairs of <br> corresponding angles are <br> congruent. |
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| Alternate Interior Angles Theorem | If two parallel lines are cut by a <br> transversal, then the pairs of <br> alternate interior angles are <br> congruent. |
| Alternate Exterior Angles Theorem | If two parallel lines are cut by a <br> transversal, then the pairs of <br> alternate exterior angles are <br> congruent. |
| Same-Side Interior Angles Theorem | If two parallel lines are cut by a <br> transversal, then the pairs of same- <br> side interior angles are <br> supplementary. |
| Same-Side Exterior Angles Theorem | If two parallel lines are cut by a <br> transversal, then the pairs of same- <br> side exterior angles are <br> supplementary. |

## Stand Alone Angle Relationships:

- Vertical Angles are always congruent.
- Linear Pair are always supplementary


## Angle Relationships based on Parallel Lines



| Angles Relationship | Type |
| :--- | :--- |
| $\angle 1 \cong \angle 5, \angle 3 \cong \angle 7$ | Corresponding |
| $\angle 2 \cong \angle 6, \angle 4 \cong \angle 8$ | Alternate Interior |
| $\angle 3 \cong \angle 6, \angle 4 \cong \angle 5$ | Alternate Exterior |
| $\angle 1 \cong \angle 8, \angle 2 \cong \angle 7$ | Same Side Interior |
| $\angle 3 \& \angle 5$ are supplements |  |
| $\angle 4 \& \angle 6$ are supplements |  |
| $\angle 1 \& \angle 7$ are supplements | Same Side EXterior |
| $\angle 2 \& \angle 8$ are supplements |  |


| Converse of Corresponding Angles <br> Theorem | If the pairs of corresponding angles <br> are congruent, then the two lines cut <br> by a transversal are parallel. |
| :--- | :--- |
| Converse of Alternate Interior Angles <br> Theorem | If the pairs of alternate interior <br> angles are congruent, then the two <br> lines cut by a transversal are <br> parallel. |
| Converse of Alternate Exterior Angles <br> Theorem | If the pairs of alternate exterior <br> angles are congruent, then the two <br> lines cut by a transversal are <br> parallel. |
| Converse of Same-Side Interior Angles <br> Theorem | If the pairs of same side interior <br> angles are supplementary, then the <br> two lines cut by a transversal are <br> parallel. |
| Converse of Same-Side Exterior <br> Angles Theorem | If pairs of same side exterior <br> angles are supplementary, then the <br> two lines cut by a transversal are <br> parallel. |

## Slopes

- Parallel lines have the same slope.
- Perpendicular lines have slopes that are opposite reciprocals. If you multiplied them together you would get -1 .


## Other theorems to use in proofs:

- Vertical Angles Congruence Thm: Vertical angles are congruent.
- Right Angles Congruence Thm: All right angles are congruent.
- Linear Pair Thm: If two angles form a linear pair, then they are supplementary.
- Congruent Complements Thm: If two angles are complementary to the same angle or congruent angles, then the angles are congruent.
- Congruent Supplements Thm: If two angles are supplementary to the same angle or congruent angles, then the angles are congruent.

