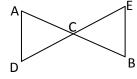
## Unit 6 Facts: Steps for Proving Triangles Congruent

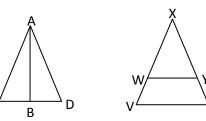
- o Mark the "Given" information on the picture. Some information to be deduced:
- o Given an Angle Bisector:
  - Mark the congruent angles on the diagram
  - Statement example: ∠ABC ≅ ∠CBD
  - Reason: Def. of Angle Bisector
- o Given a Segment Bisector:
  - Mark the congruent segments on the diagram
  - Statement example:  $\overline{AC} \cong \overline{CB}$
  - Reason: Def. of Segment Bisector
- o Given a Midpoint:
  - Mark the congruent segments on the diagram
  - Statement example:  $\overline{AC} \cong \overline{CB}$
  - Reason: *Def. of Midpoint*
- o Given Perpendicular Lines:
  - Mark right angle on diagram
  - Statement ∠ABC is a right angle, ∠ABD is a right angle example:
  - Reason: Def of Perpendicular lines
- o Given Parallel Lines:
  - Mark congruent angles
  - Statement  $\angle 1 \cong \angle 2$  example:
  - Reason: Alt Int ∠s Thm
- o Isosceles Triangles:
  - Mark congruent segments and congruent angles
  - Statement:  $\overline{AB} \cong \overline{BC}$  and  $\angle A \cong \angle C$
  - Reason: Def of Isosceles Triangle (for congruent segments) and Isosceles Triangle Theorem (for congruent ∠'s)



## 2. Look for congruencies not in Given.

- $\circ$  Vertical Angles: (Vertical angles form an "X" and the angles across from each other are  $\cong$ )
  - Mark congruent angles on the diagram
  - Statement: ∠ACD ≅ ∠BCE
  - Reason: Vertical Angles Theorem
- Shared lines, segments, or angles:
  - Mark congruent segments or angles on the diagram
  - Statement:  $AB \cong AB$  or  $\angle X \cong \angle X$
  - Reason: Reflexive Property





## 3. Look at what you marked in the picture: how are the triangles congruent?

- SSS: 3 sides are marked congruent
- o SAS: 2 sides and an included angle are marked congruent
- o ASA: 2 angles and an included side are marked congruent
- o AAS: 2 consecutive angles and a non-included side are marked congruent
- o HL: In 2 right triangles, a leg and the hypotenuse are marked congruent

## 4. Look at "Prove Line". Were you trying to prove two triangles are congruent?

If so, then you are done. If not, then...

- o Proving certain parts are congruent:
  - Statement: *part* ≅ *part*
  - Reason: CPCTC
- o Proving lines parallel:
  - Statement: *line*//*line*
  - Reason: (Could be any of the following):
    - Converse of alt int ∠ 's theorem
    - Converse of alt ext ∠ 's theorem
    - Converse of ss int ∠ 's theorem
    - Converse of ss ext ∠ 's theorem
    - Converse of corresponding ∠ 's postulate
  - o Proving other things besides parts congruent (always goes one step beyond CPCTC):
    - Statement example: C is the midpoint of  $\overline{AC}$
    - Reason: Definition of midpoint